

NAME: \_\_\_\_\_

(1) Evaluate  $\lim_{x \rightarrow \infty} -3x^5 + 6x^2 - 7$

(2) Find a value of  $k$  so that  $\lim_{x \rightarrow \infty} \frac{3x^4 + 7x - 7}{kx^4 - 11} = \frac{1}{2}$ .

(3) Find a value of  $k$  so that  $\lim_{x \rightarrow -\infty} \frac{-3x^4 + 7x - 7}{5x^k - 11} = \infty$ .

(4) Consider the piecewise function  $f$ , defined by

$$f(x) = \begin{cases} \frac{1}{x} & \text{if } x < 0, \\ 2 & \text{if } 0 \leq x < 2, \\ 3 & \text{if } x = 2, \\ (2x - 2) & \text{if } x > 2. \end{cases}$$

(a) NEATLY sketch the graph of  $f$ .

(b) Evaluate the following limits. If a limit does not exist, write "DNE".

(i)  $\lim_{x \rightarrow -\infty} f(x) =$

(ii)  $\lim_{x \rightarrow 0} f(x) =$

(iii)  $\lim_{x \rightarrow 2} f(x) =$

(iv)  $\lim_{x \rightarrow \infty} f(x) =$

(v)  $\lim_{x \rightarrow 1} f(x) =$

(vi)  $\lim_{x \rightarrow 3} f(x) =$